

# Accretion in Clusters

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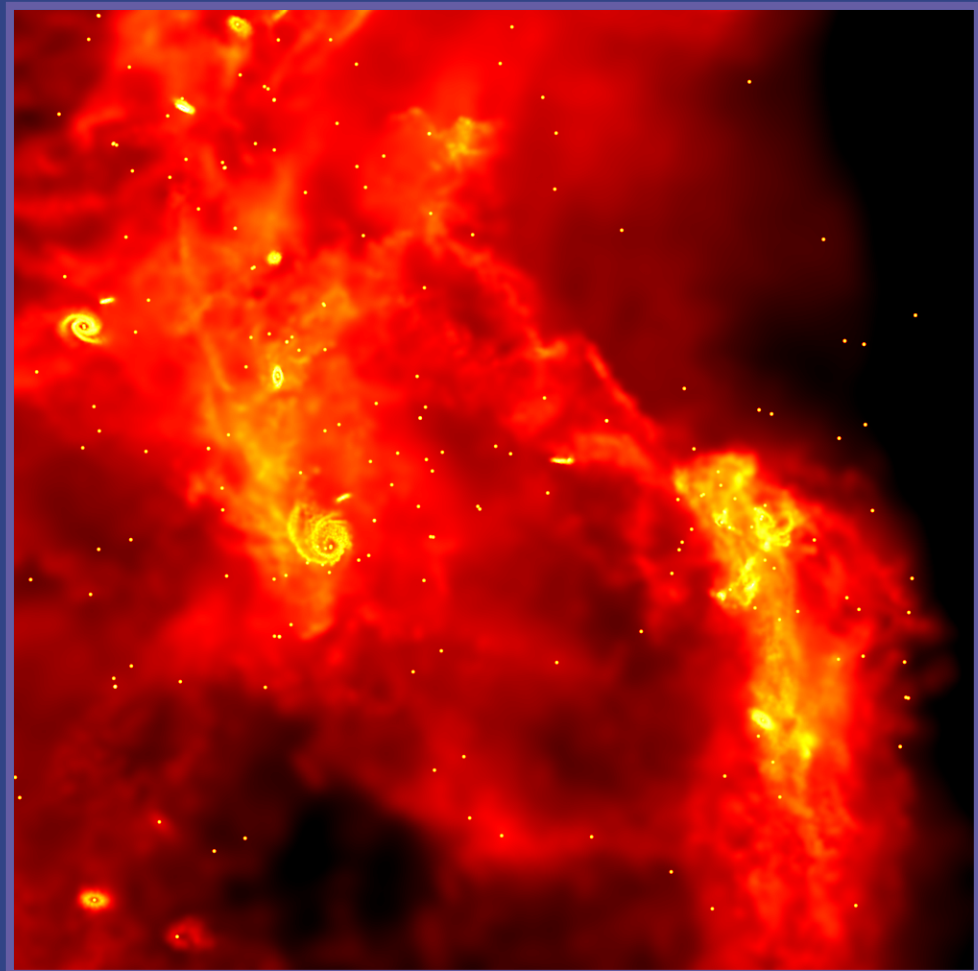
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Andrews)



UK Astrophysical  
Fluids Facility

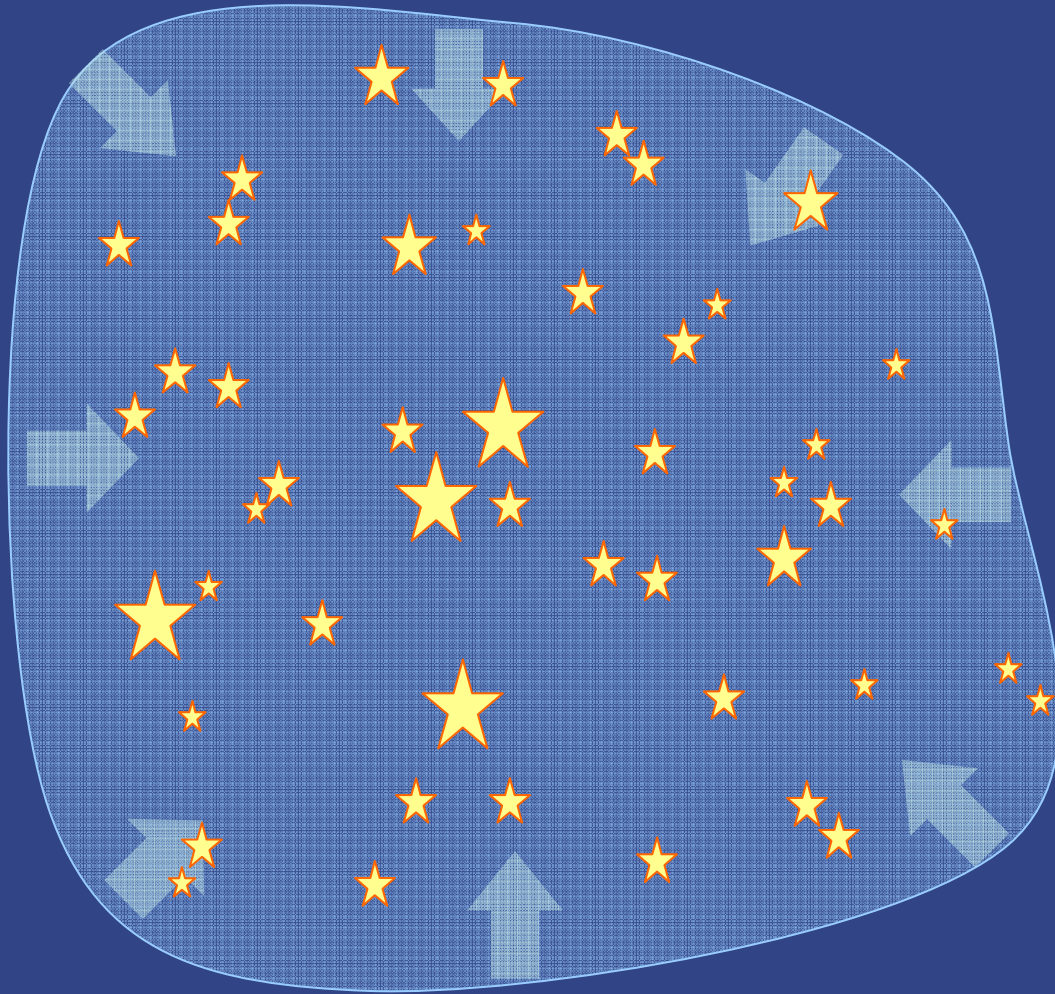


On what scale is accretion  
most important?

What determines the IMF?

# IMF from competitive accretion

Collapsing proto-cluster core



- Bound region forms and starts to collapse.
- Fragmentation of molecular cloud sets the **seeds** for the formation of young system.
- Subsequent accretion from the cloud shapes the masses of the stars.
- Dynamic process.
- IMF **grows (but always has the same shape)!**

# Accretion and the IMF...

Accretion rate:  $\dot{M}_* = \pi \rho V_{\text{rel}} R_{\text{acc}}^2$

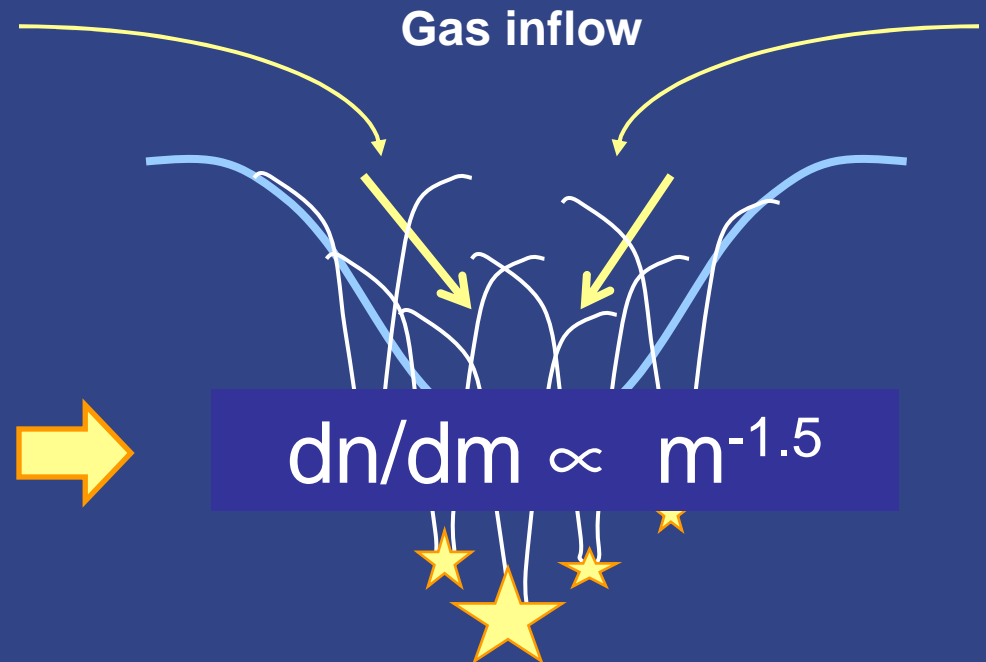
- Initially, fragmentation occurs as gas falls into the protocluster core potential. Low relative velocity between gas and protostellar embryos:

$$R_{\text{tidal}} \approx 0.5 \left( \frac{M_*}{M_{\text{enc}}} \right)^{1/3} R,$$

- Once the protostars dynamically interact, their motions are determined by encounters. Accretion is now defined by the Bondi-Hoyle radius:

$$R_{\text{BH}} = 2GM_*/(V_{\text{rel}}^2 + c_s^2)$$

Bonnell et al 2001a,b



$$dn/dm \propto m^{-2.5}$$



# Accretion and the IMF...

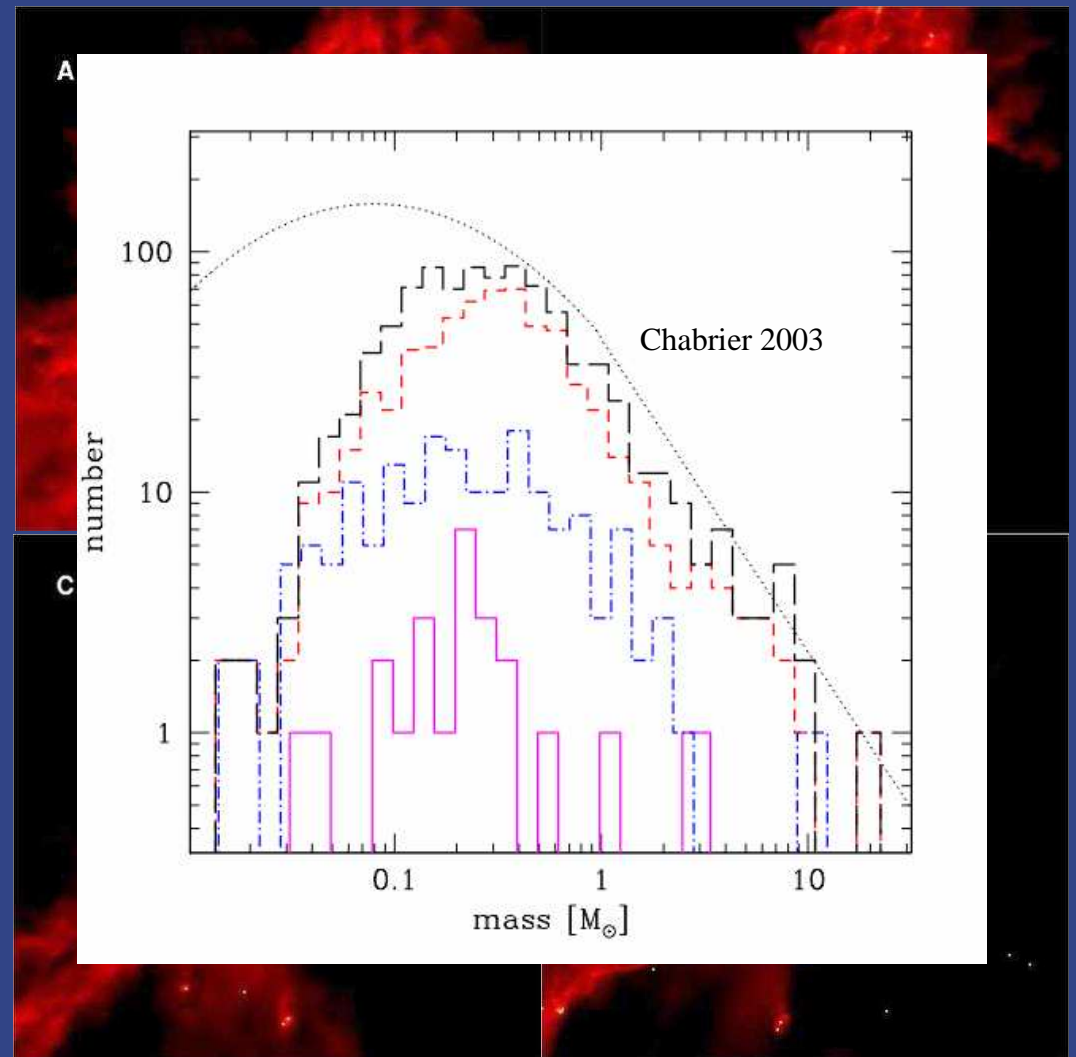
Bonnell, Vine & Bate 2004

- Once the first protostellar encounters:

Combination of tidal and BH accretion

Protostellar mass function grows with time, but is always

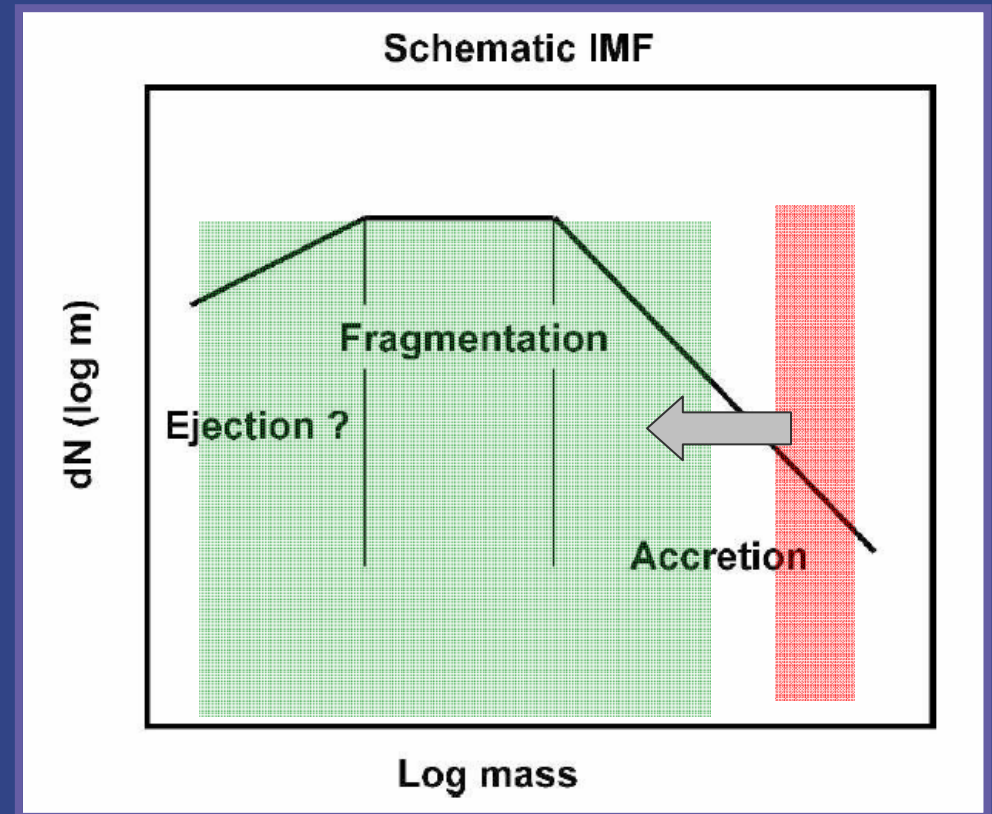
consistent with the IMF.  
Creates a naturally mass segregated cluster.



# Accretion and the IMF...

- 3 processes control the full IMF in the cluster accretion process:

- Fragmentation
- Accretion
- Ejection



- All parts of the IMF depend on each other.

# Conditions for competitive accretion...

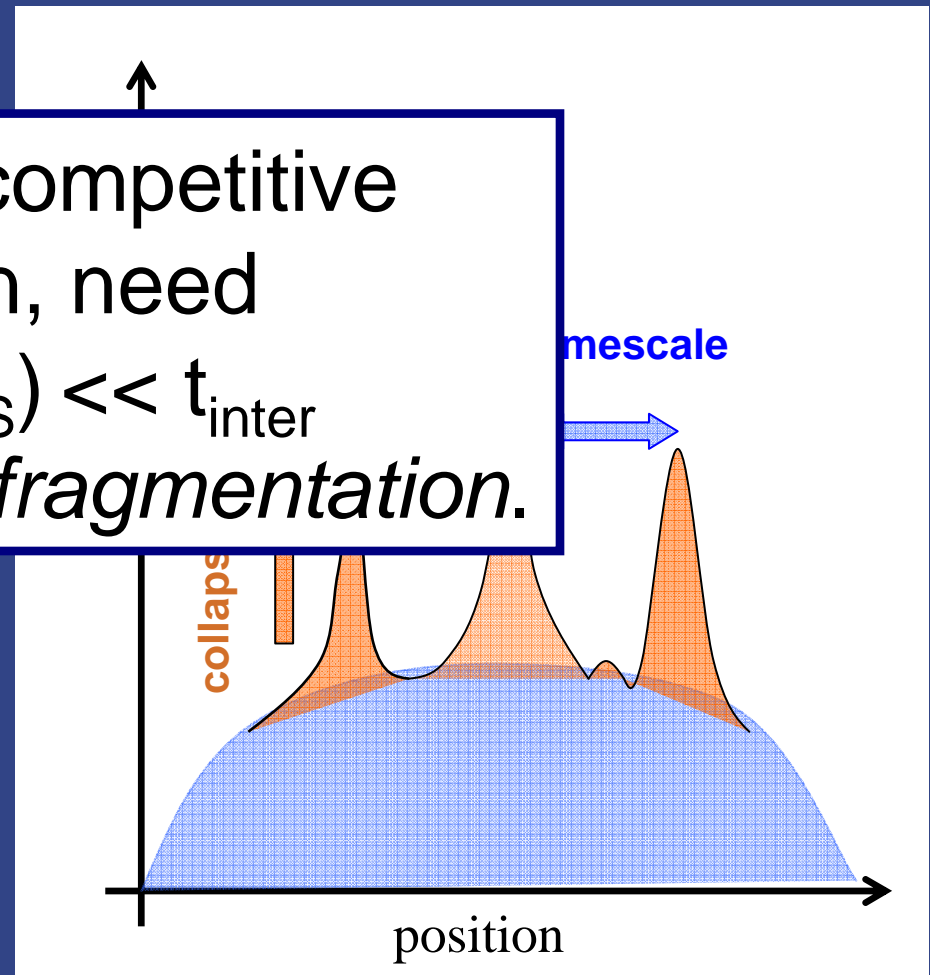
- Competitive accretion requires a region in which the collapse time is much shorter than the interaction time.

- If the clouds have similar cloud densities and masses, then...

$$t_{\text{inter}} \sim t_{\text{coll}} \sim t_{\text{ff}}$$

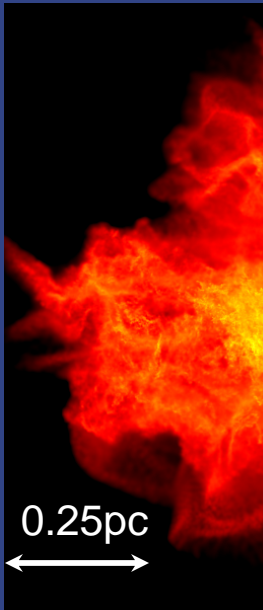
- Any region with multiple Jeans masses automatically satisfies this requirement.

To prevent competitive accretion, need  
 $t_{\text{coll}} \text{ (or } t_{\text{PMS}}) \ll t_{\text{inter}}$   
*at the **onset** of fragmentation.*

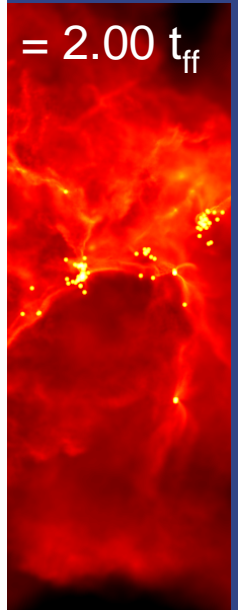
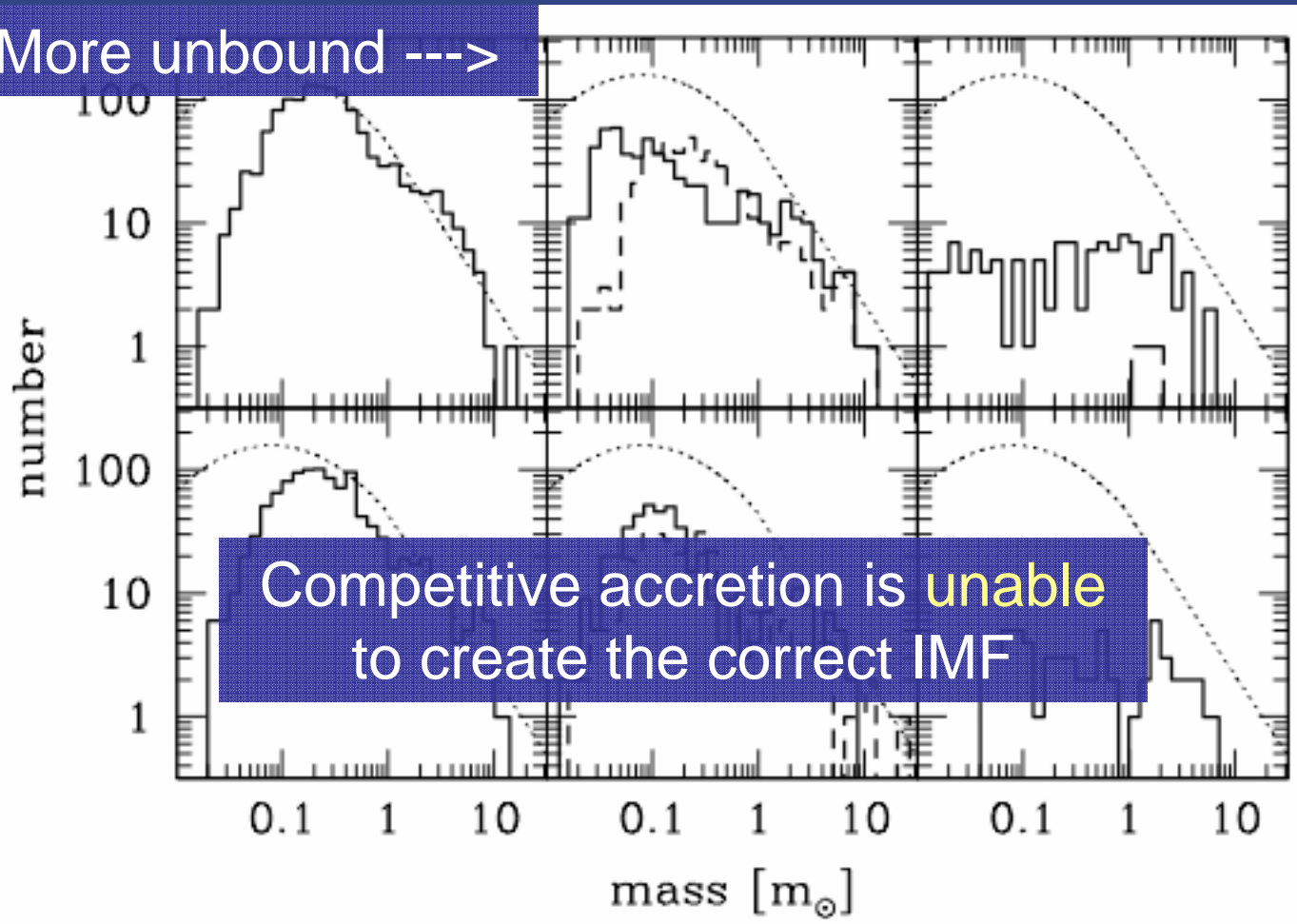


# What happens when regions don't interact?

Take a  
energy



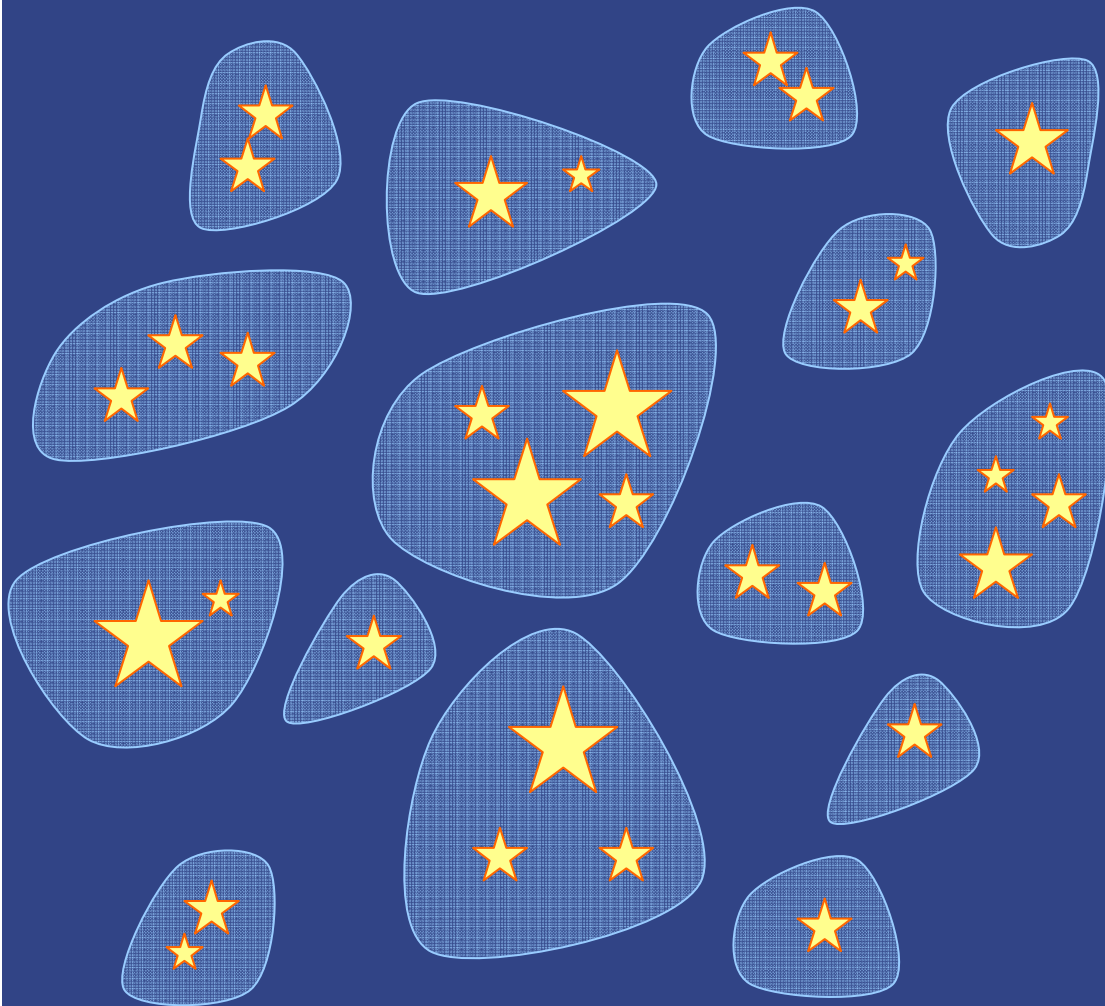
More unbound --->



Clark et al (2007)

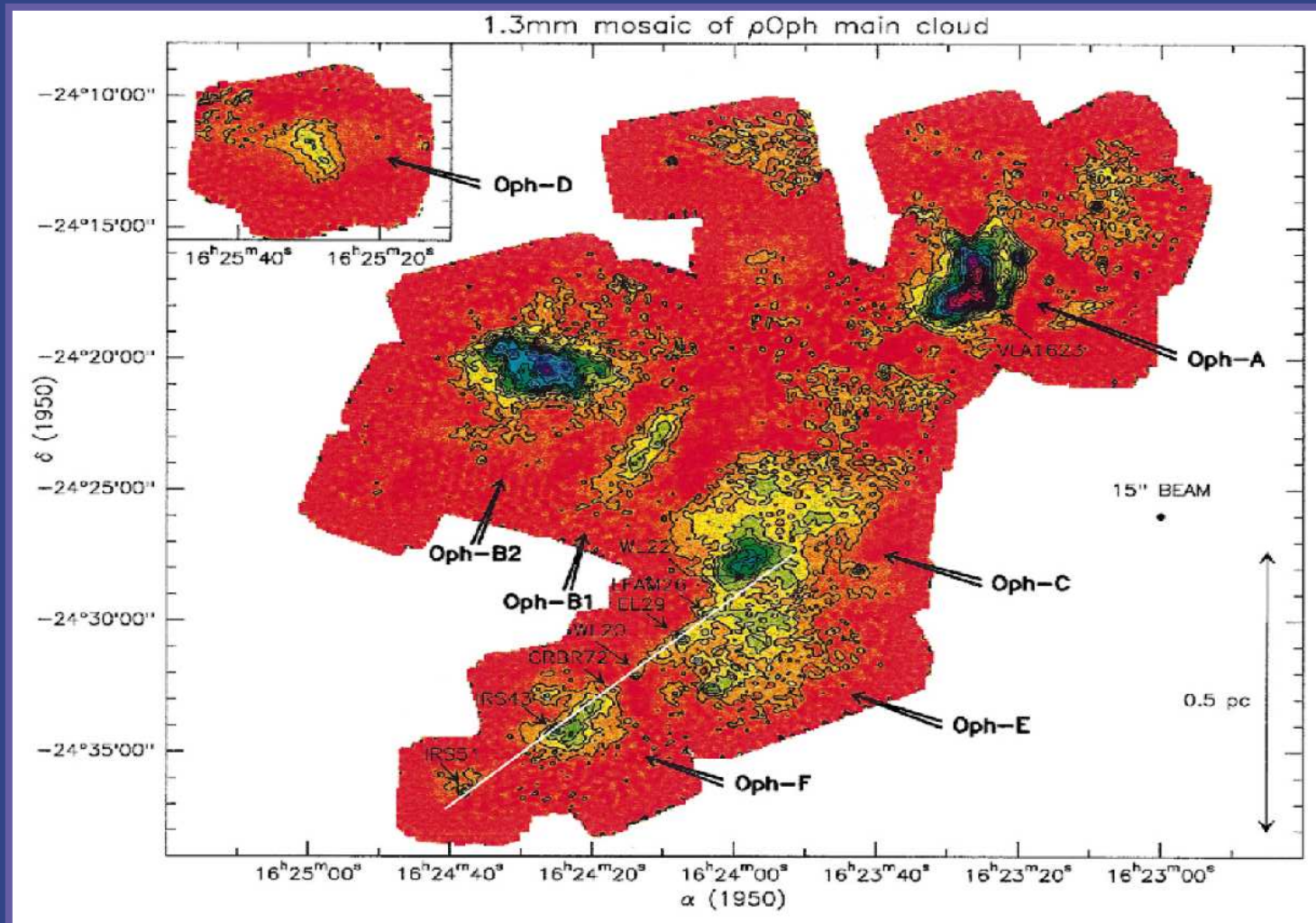


# IMF from fragmentation



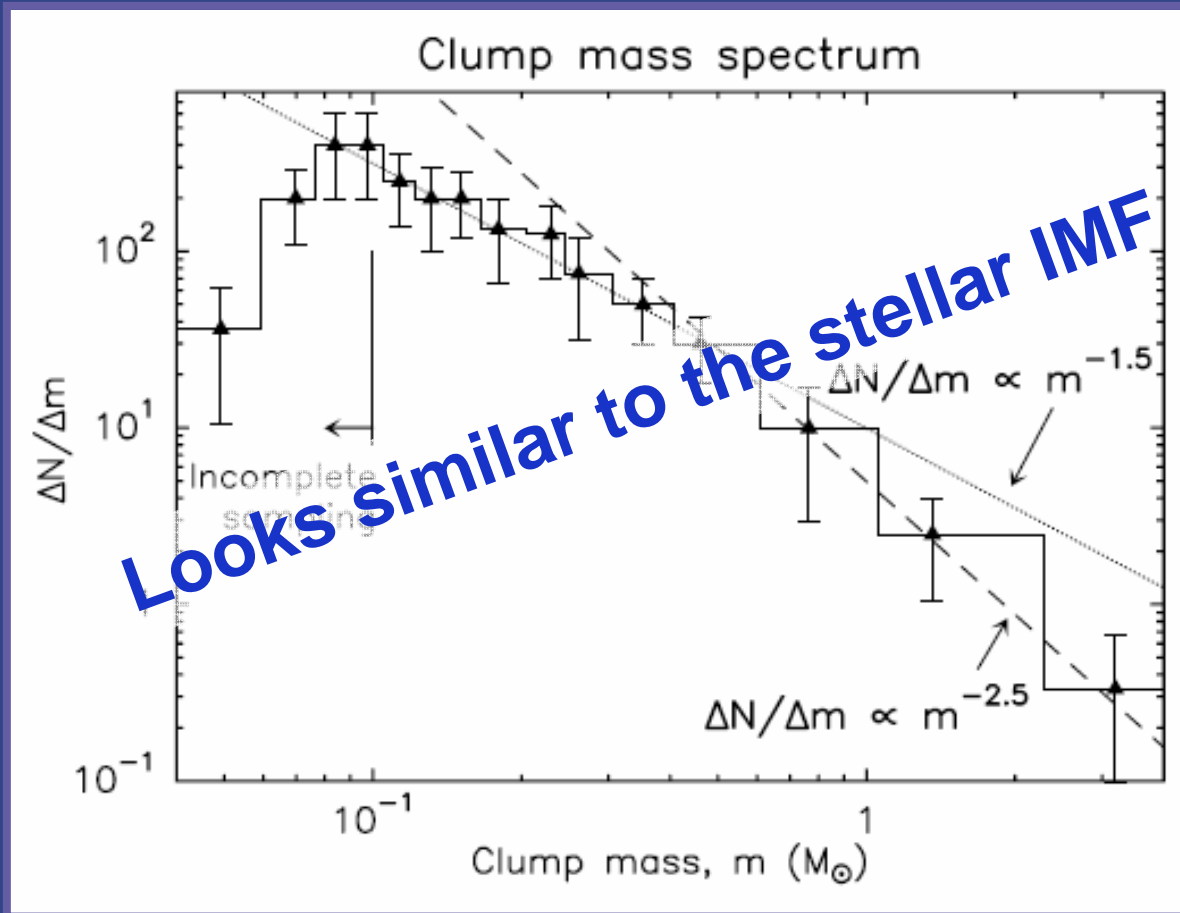
- Fragmentation of molecular cloud sets the mass for star formation **locally**.
- Subsequent accretion from the cloud is unnecessary/unimportant .
- Static process.
- IMF is **primordial**.

# The IMF from fragmentation



*Motte, André & Neri 1998, A&A 336, 150*

# The IMF from fragmentation



Similar results:

Testi & Sargent (1998)

Johnstone et al (2000, 2001, 2006)

Nutter & Ward-Thompson (2006)

Lada et al 2006

*Motte, André & Neri 1998, A&A 336, 150*

# Observational predictions

## Accretion IMF...

- Cloud should be undergoing global collapse (and thus global contraction; see above bound).
- Some degree of mass segregation should be visible.
- Interaction timescales are comparable to the PMS timescale.
- Massive, pre-protostellar cores should be fairly rare.

## Fragmentation IMF...

- Cloud appears not to be undergoing fragmentation.
- No clear reason why mass segregation should exist in the PMS phase.

ALMA will provide the line-widths at the necessary scales (all!) to help distinguish between these two contrasting pictures.

# Competitive accretion **within** the fragmentation model?

What if the clump MF is the  
origin of the system IMF?

- Highly likely that each bound 'clump' will form more than one star (Andre et al 2000; **Goodwin et al 2004a,b**; Goodwin & Kroupa 2005).
- Observations show that multiplicity of embedded protostellar objects is higher than in the field star population (Duchene et al 2004; Correia et al 2006)
- More massive clumps may be unstable to fragmentation during collapse (Andre et 2000).
- **Competitive accretion?**

# Core fragmentation test

1000 au



QuickTime™ and a  
GIF decompressor  
are needed to see this picture.

# Accretion rates

- From self-similar collapse ( $1/r^2$  profile, Shu, Adams & Lizano 1987):  $dm/dt \sim 0.98c^3/G$
- However many authors have shown that the accretion is higher than this: e.g. Foster & Chevalier 1993; Basu (1997); Ogino et al (1999); Whitworth & Ward-Thompson (2001), Motoyama & Yohsida (2003); Banerjee & Pudritz (2007).
- Typically caused by deviation from the ( $1/r^2$ ) profile for the inner region: so called Larson-Penston solution (Larson 1969; Penston 1969), but then **rate declines exponentially**.
- More mass in the inner region than self-similar model.
- Consistent with the observations: e.g. Bontemps et al (1996); Myers et al (1998); Brown & Chandler (1999).

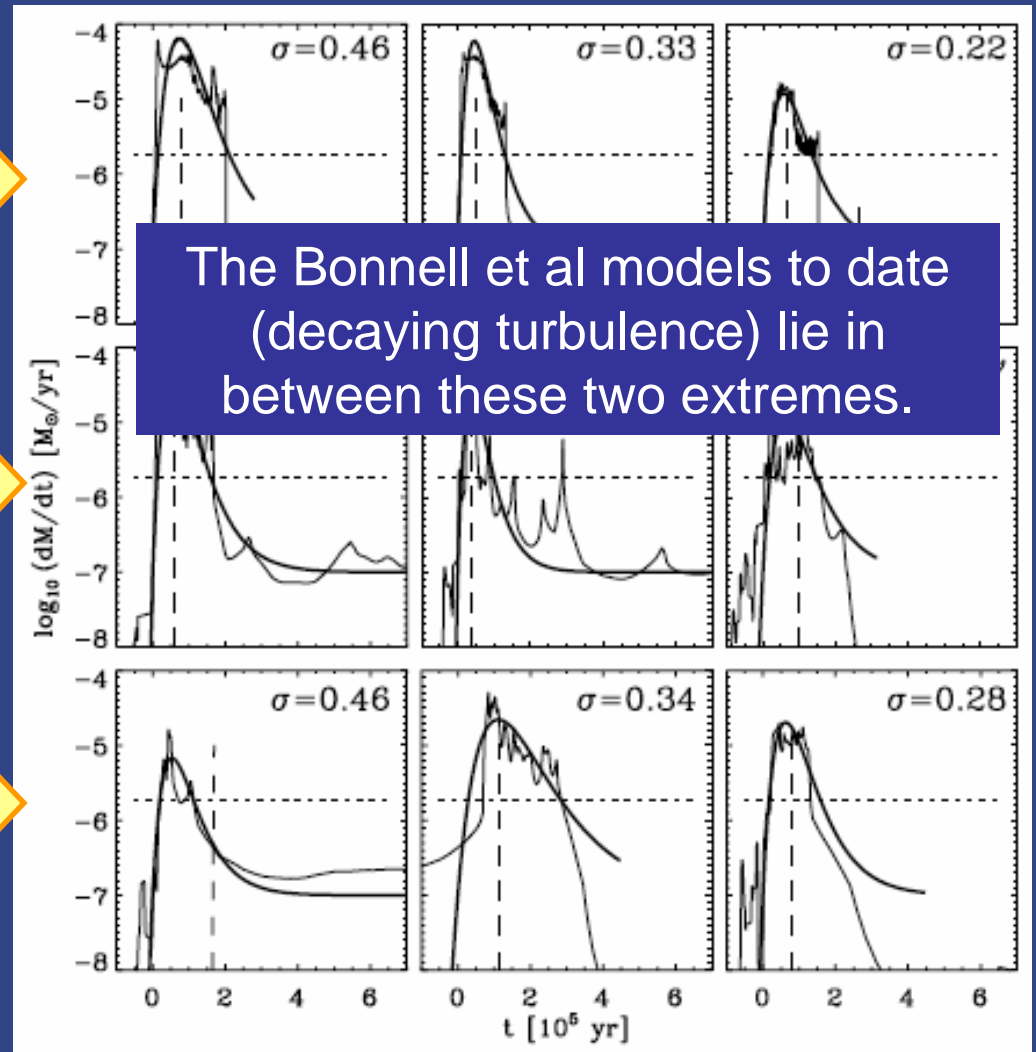


# Accretion rates

Schmeja & Klessen (2004),  
looked at simulations by  
Klessen:

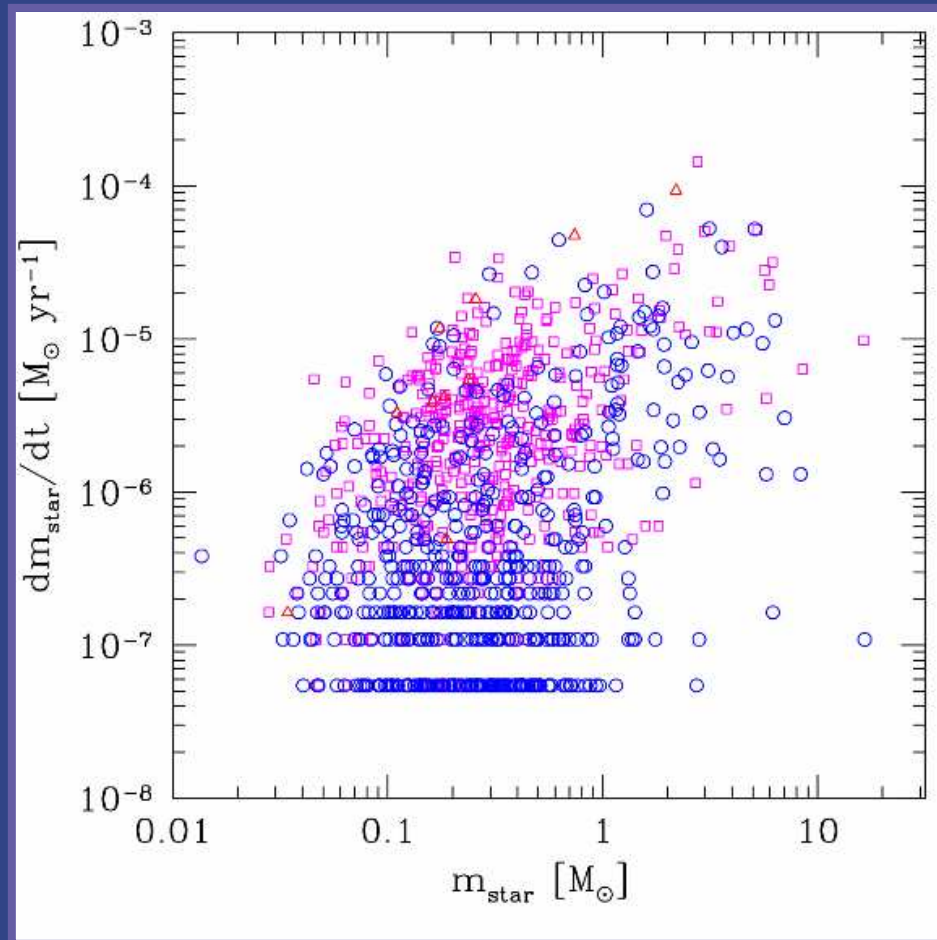
- 1) Gaussian density fluctuations, no kinetic support. Highly clustered environment.
- 2) Large scale driving. Support on large scales. Highly clustered environment.
- 3) Small scale driving: support on small scales. Comparatively isolated star formation.

$$\log \dot{M}(t) = \log \dot{M}_0 - \frac{t}{\tau}$$





# Accretion rates



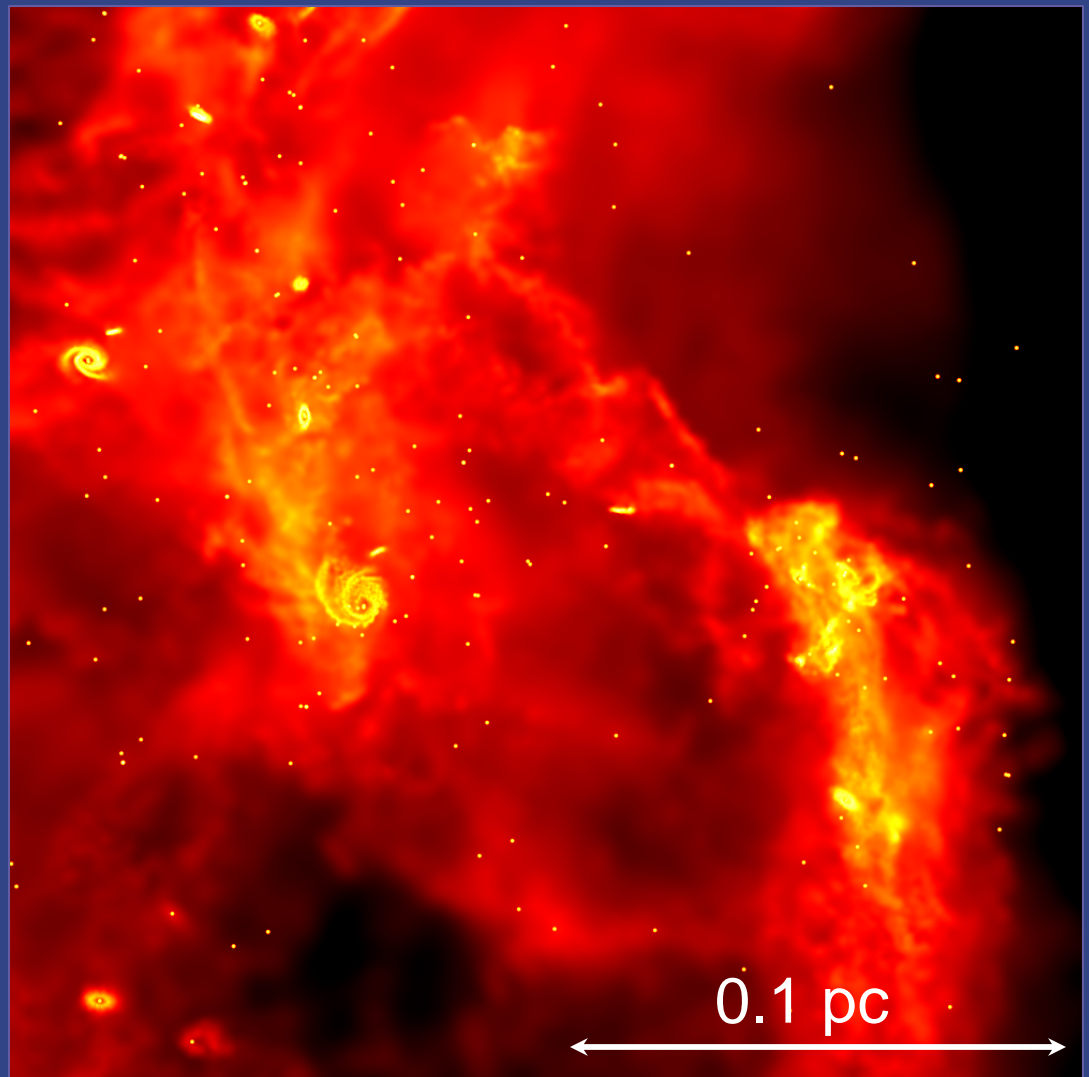
- In competitive accretion, the accretion rates are **not constant**.
- But result is complicated, since some objects are in the tidal lobe accretion phase, while others are in BH phase.
- Also sensitive to:
  - local density (BH)
  - volume averaged densities (tidal)

# Discs in dense clusters

- Originally assumed that a densely clustered environment would destroy discs (Bonnell et al 2003)...

**...Not true!**

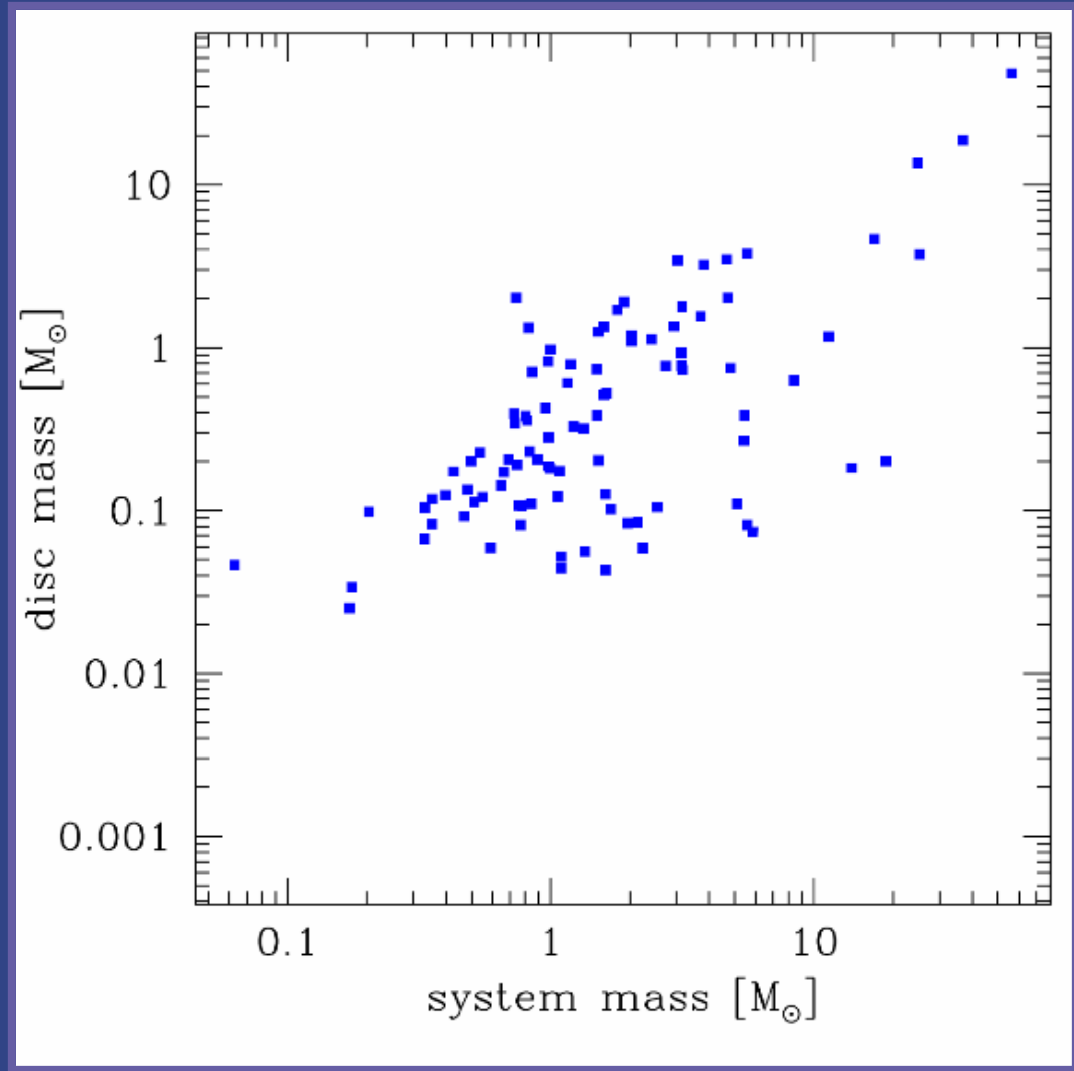
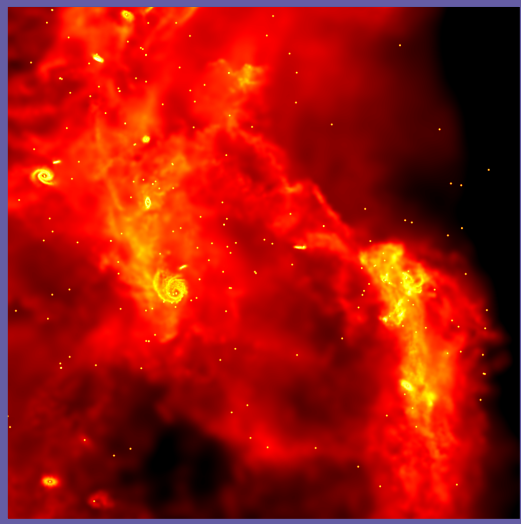
- Higher resolution simulations show that discs can survive even these extreme conditions.
- Good news, since most stars are formed in massive clusters (Lada & Lada 2003).



# Discs in dense clusters

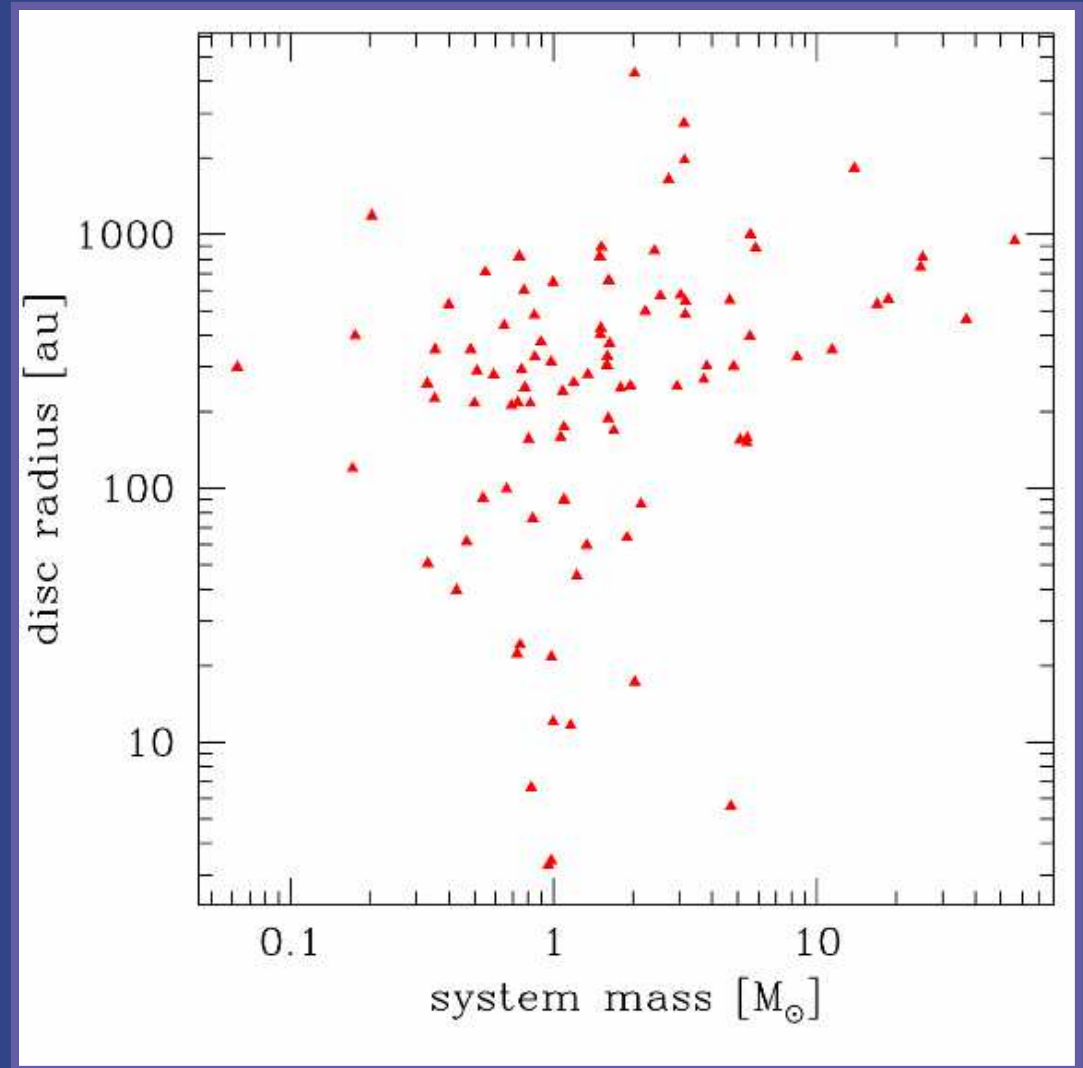
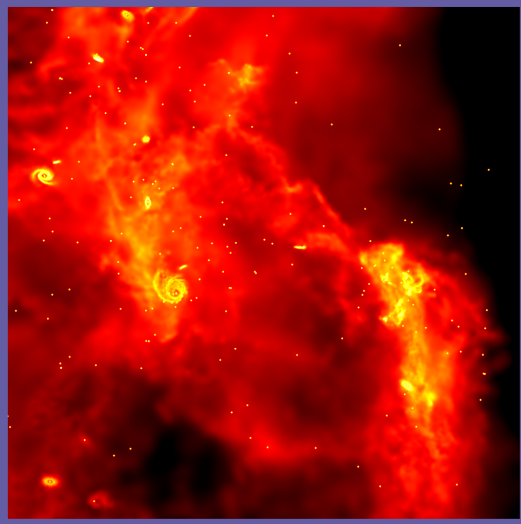
- Relationship between disc mass and protostellar system mass:

$$m_{\text{disc}} \propto m_{\text{sys}}^{1.5 - \frac{1}{2}}$$

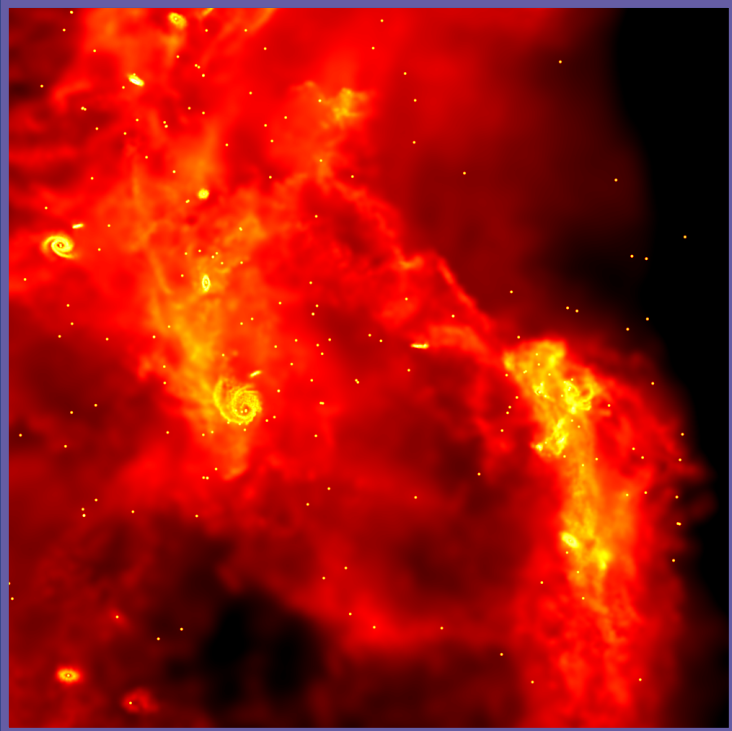


# Discs in dense clusters

- However the relationship between the disc radius and the system mass is **not so clear!**



# Discs in dense clusters



- Turbulence causes neighbouring regions to have different local angular momentum:

Discs seen with a variety of projections.

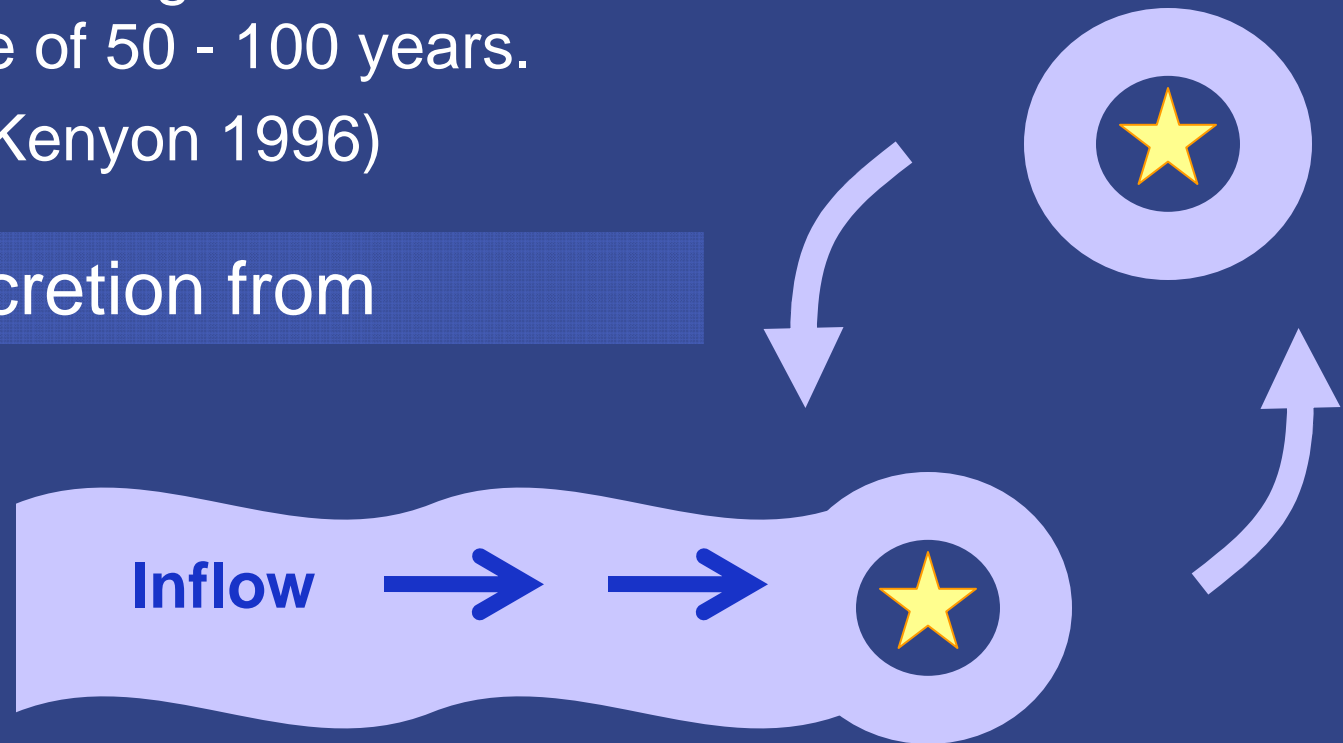
- Protostars/systems can lose their discs via interactions, but can rapidly accrete new ones, provided they are still in a dense enough environment.
- New discs are not necessarily aligned to the rotational plane of the protostars/systems.

# FU Orionis objects?

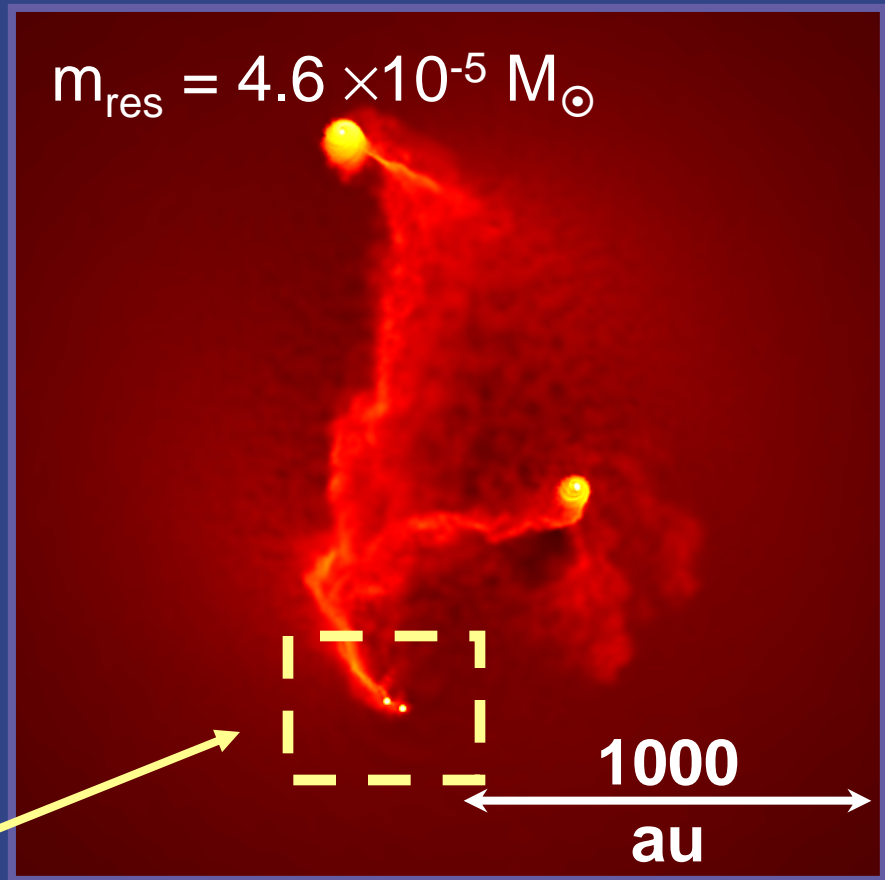
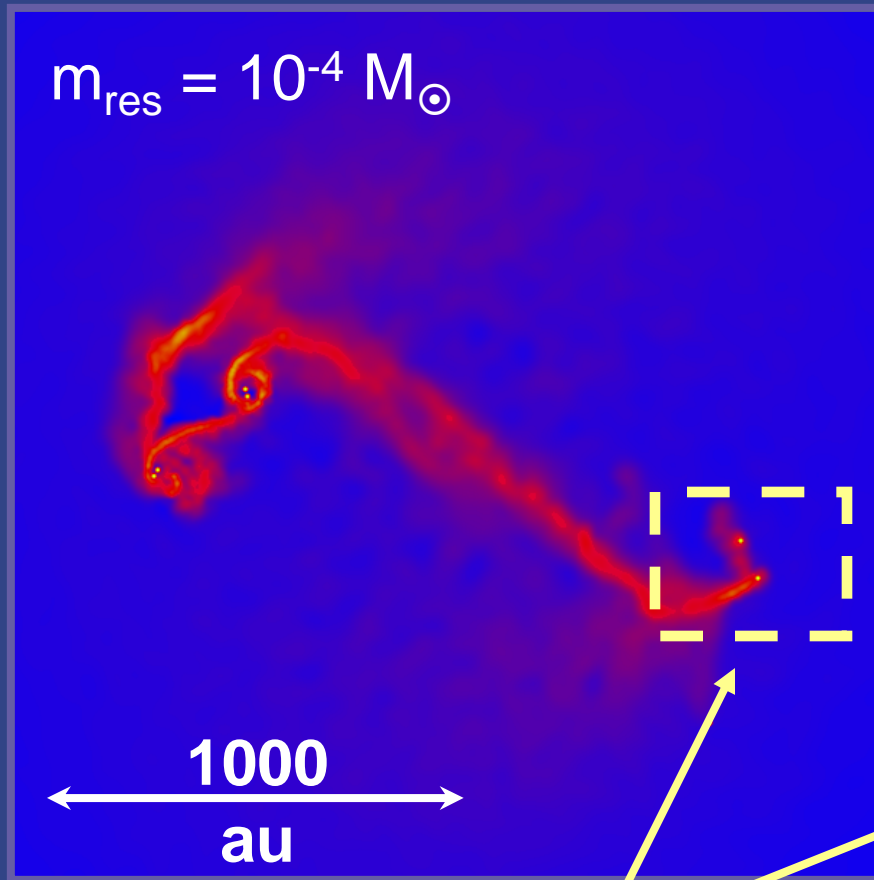
## Properties...

- Occurs in young embedded systems
- High accretion rates  $\sim 10^{-4}M_{\odot} \text{ yr}^{-1}$
- Decay from this high accretion occurs on a timescale of 50 - 100 years.  
(Hartmann & Kenyon 1996)

...binary accretion from filament?



# FU Orionis objects?

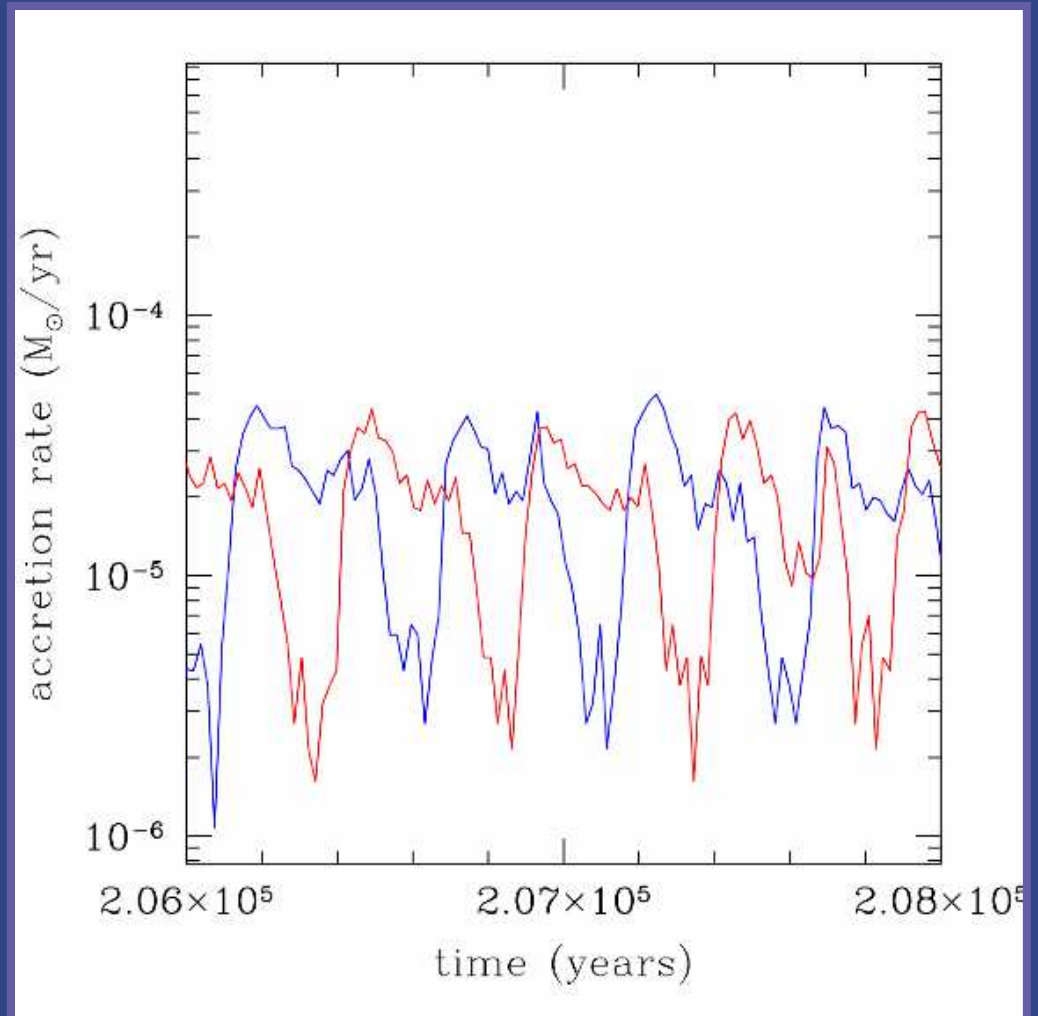
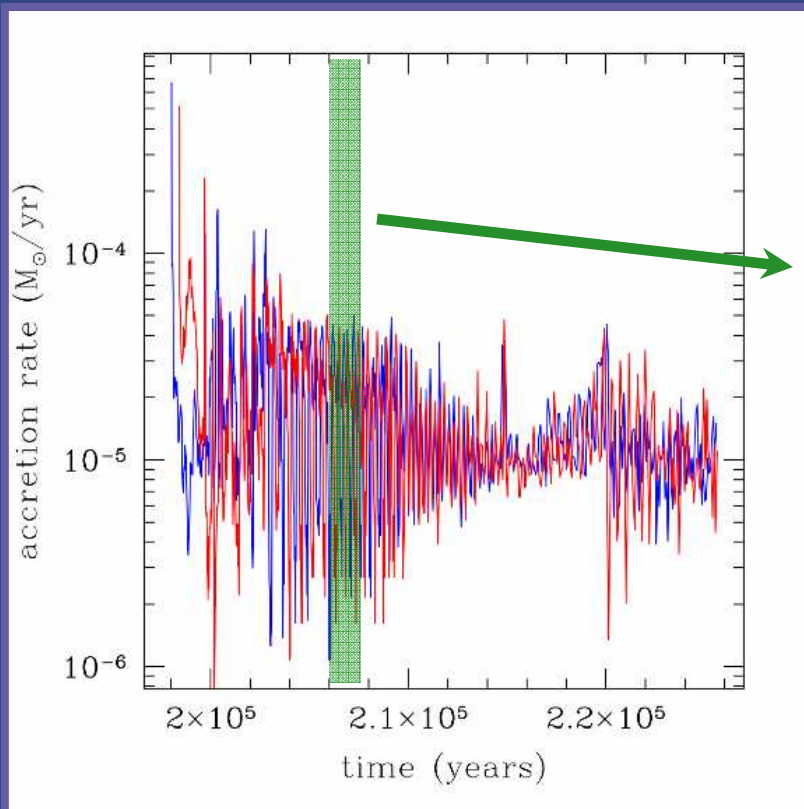


We ran two simulations: found at least two such examples!



# FU Orionis objects?

... binary accretion from filament?

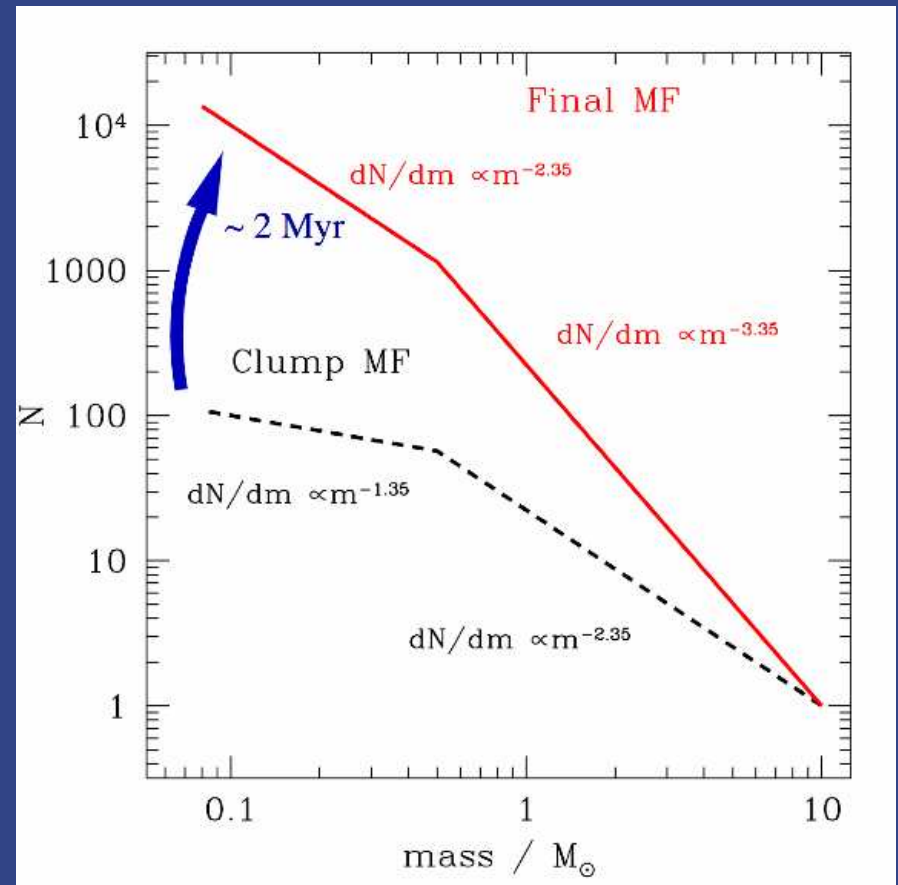
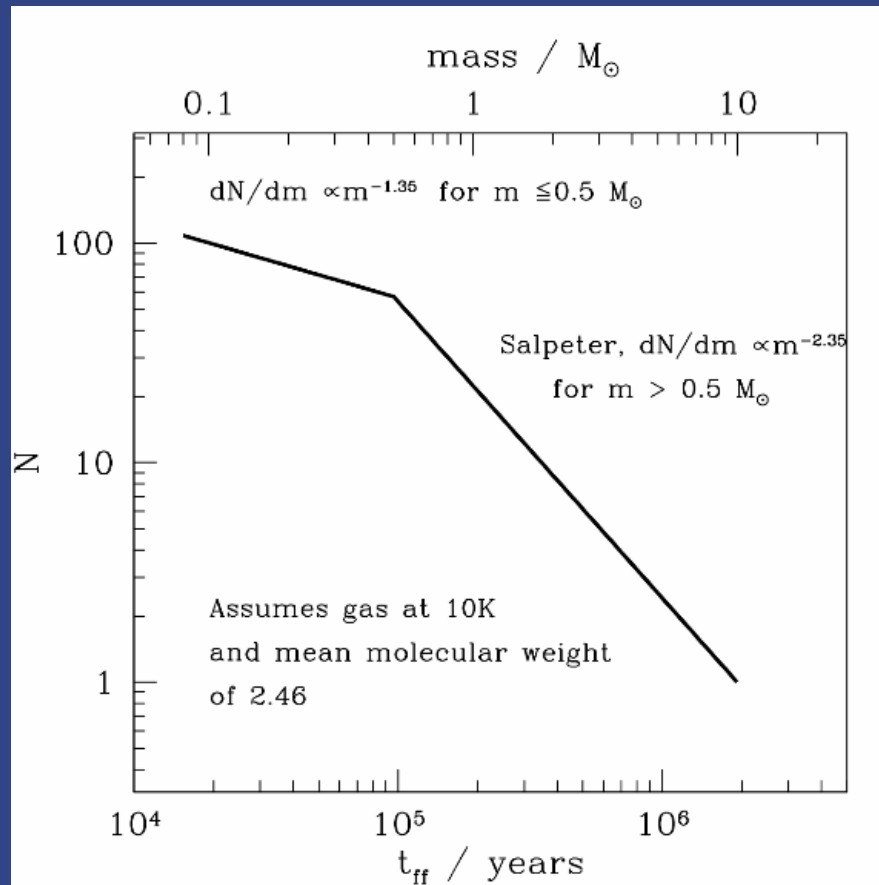




# Conclusions...

- With better maps of the velocity structure in star forming regions, ALMA will help distinguish between global accretion and local accretion -> IMF formation.
- What fraction of the CMFs constitute **bound** pre-protostellar cores?
- Should also be able to test whether the disc properties predicted by competitive accretion are realistic!
- Does competitive accretion dominate on small scales
- How much structure is there at the 100 AU scale in protostellar cores?

# A timescale problem?



*Clark, Klessen & Bonnell  
2007*

# Stability of sub-mm clumps

- The stability of clumps seen in the sub-mm observations is **very sensitive to the assumed dust temperature.**

$$N_{\text{H}_2} \propto 1/T_{\text{dust}} \rightarrow M_{\text{clump}} \propto T_{\text{dust}}^{-1}$$

Jeans mass:  $m_{\text{J}} \propto [T_{\text{gas}}]^{3/2} [\rho]^{-1/2}$  and again  $\rho \propto T_{\text{dust}}^{-1}$

So the **inferred** jeans mass in the clump depends on **assumed** dust temperature:

$$m_{\text{J}} \propto T^{3/2} (T^{-1})^{-1/2} \propto T^2$$

Observed stability is then the number of Jeans masses:

$$N_{\text{J}} = M_{\text{clump}}/m_{\text{J}} \propto T^{-1} \times T^{-2} \propto T^{-3}$$

**ALMA --> LINE-WIDTHS!**

# Thermal properties of the gas

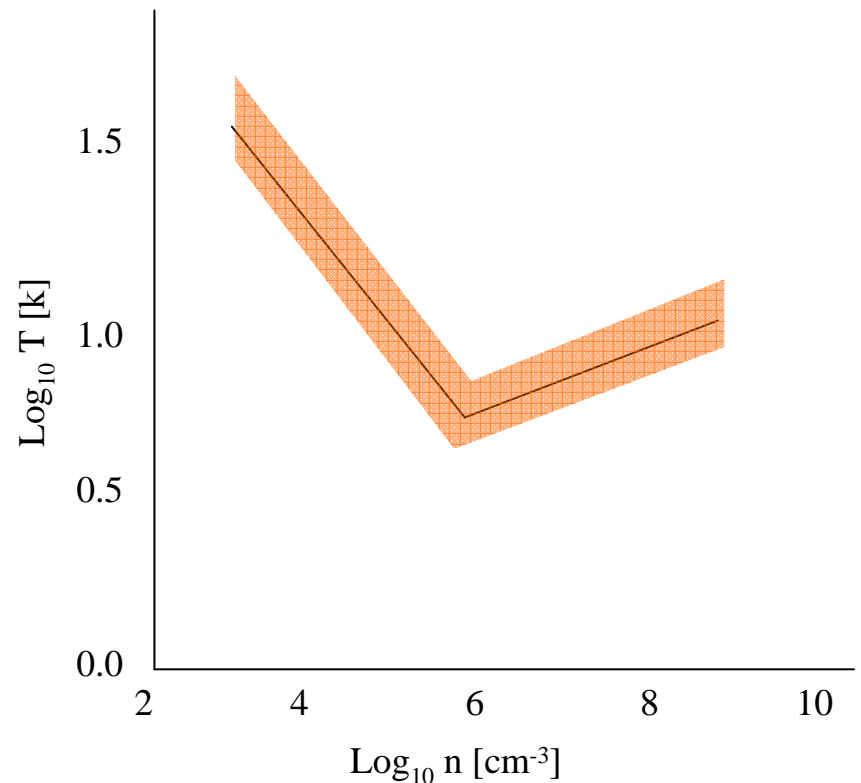
Larson (1985, 2005) suggested that the typical stellar mass may be set by a heating and cooling processes in the molecular gas. Suggested a characteristic Jeans mass, controlled by a special density and temperature:

$$T = 4.4 (\rho / 10^{-18})^{-0.27} \text{ K} ,$$

$(\rho < 10^{-18} \text{ gcm}^{-3})$

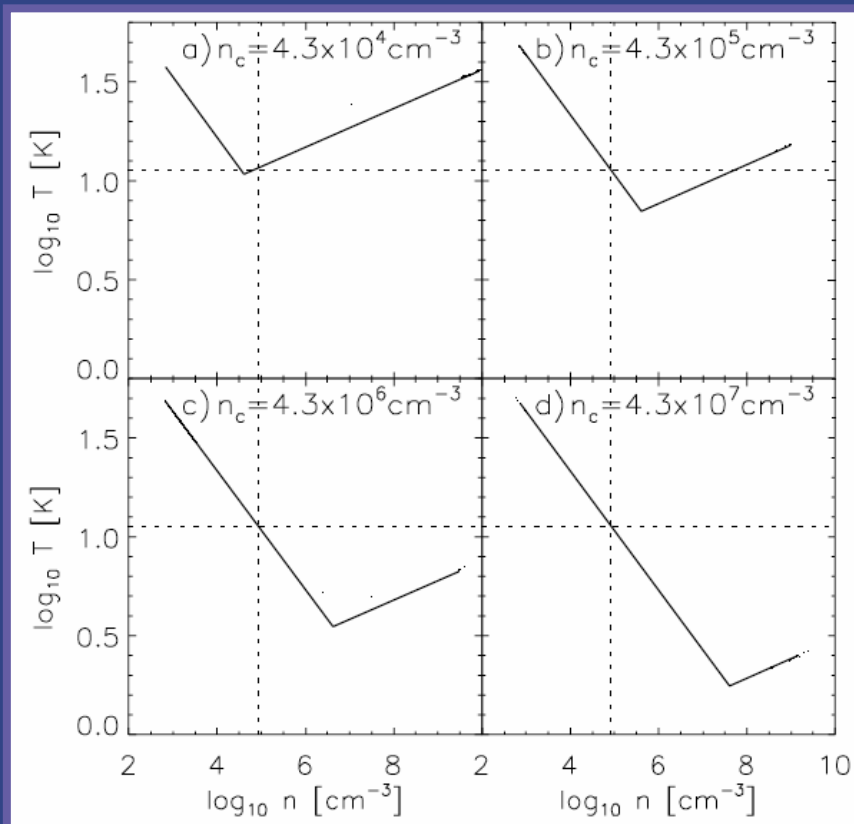
$$T = 4.4 (\rho / 10^{-18})^{+0.07} \text{ K} ,$$

$(\rho > 10^{-18} \text{ gcm}^{-3})$

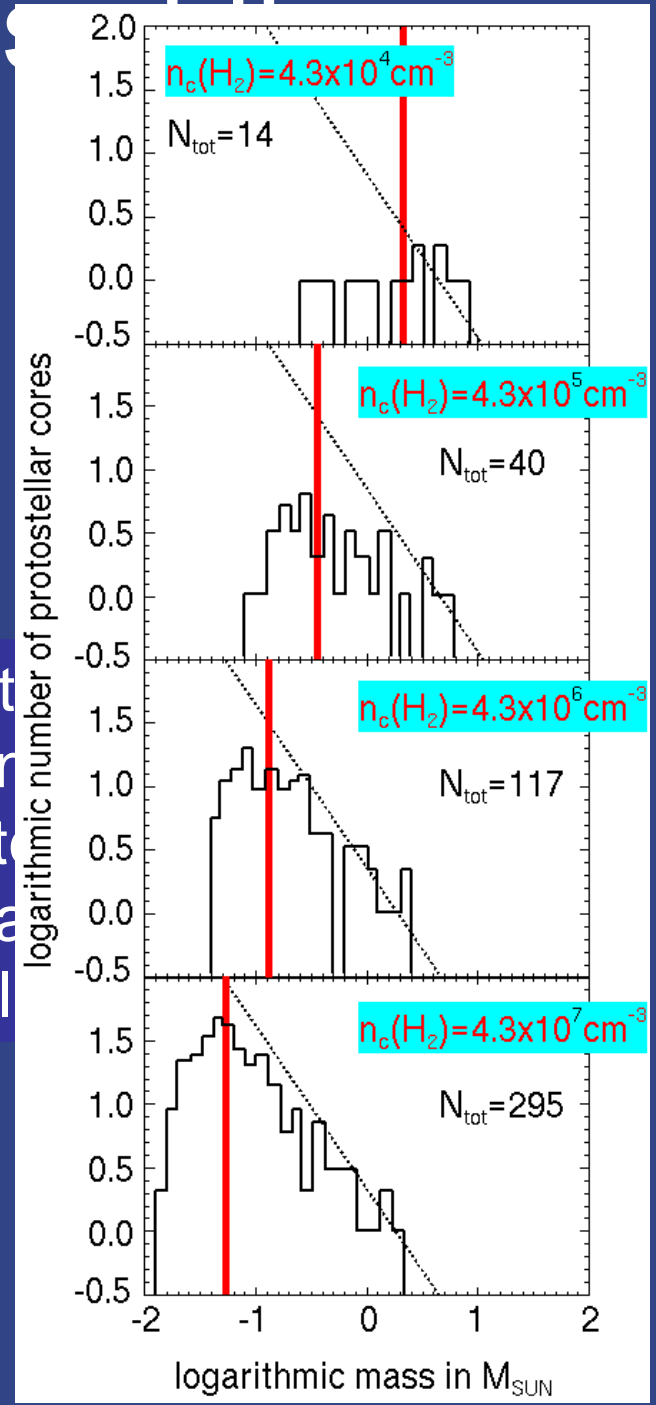


# Thermal properties of gas

Jappsen et al (2005) investigated this idea in detail with simulations of driven turbulence.

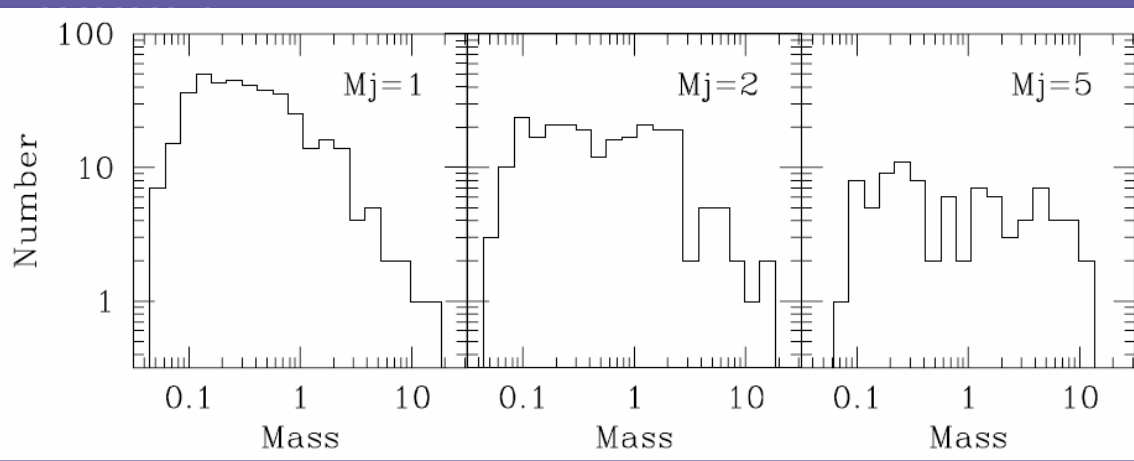


Found that turbulent character of protostellar thermal



# Good news for accreting the IMF

Bonnell, Clarke & Bate

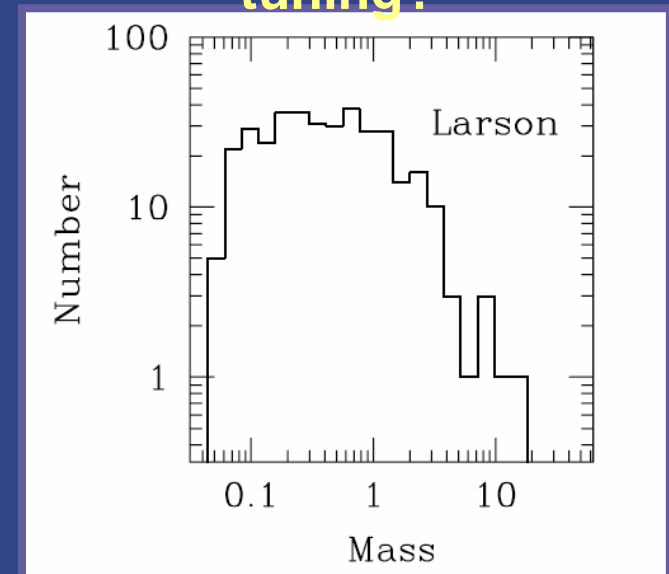


Found that changing the initial Jeans mass in the set-up, alters the position of the 'knee' in the IMF.

**Does competitive accretion really need such fine tuning?**

**Not if Larson is correct:**

Using an equation of state similar to that proposed by Larson (2005), the cloud is able to generate a more typical IMF, even from a cloud with much lower initial densities and higher initial temperatures.



# Core fragmentation test

Initial conditions:

$$3M_{\odot}; m_J = 1 M_{\odot}; \rho = 2 \times 10^{-19} \text{g cm}^{-3}$$

$$\alpha \sim 0.48; \quad \beta \sim 0.02$$

Uniform sphere at

EOS:  $p \propto \rho^{\gamma}$

$$\rho < 10^{-15} \quad \gamma = 1.0$$

$$10^{-15} < \rho < 10^{-13} \quad \gamma = 1.1$$

$$10^{-13} < \rho < 10^{-11} \quad \gamma = 1.4$$

$$10^{-11} < \rho \quad \gamma = 1.0$$

$$2 \times 10^6 \text{ SPH particles: } m_{\text{res}} = 4.6 \times 10^{-5} M_{\odot}$$